

1) The electronic polarizability of the Ar atom has a value of  $1.7 \times 10^{-40} \text{ F m}^2$ . What is the static dielectric constant of the solid Ar if its density is  $1.8 \text{ g cm}^{-3}$  and its atomic mass is  $39.95 \text{ g mol}^{-1}$ ? (Avogadro's number =  $6.02 \times 10^{23} \text{ mol}^{-1}$ ).

2) Consider a CsCl crystal which has CsCl unit cell crystal structure (one  $\text{Cs}^+ \text{Cl}^-$  pair per unit cell) with a lattice parameter (a) of  $0.412 \text{ nm}$ . The electronic polarizability of  $\text{Cs}^+$  and  $\text{Cl}^-$  ions are  $3.35 \times 10^{-40} \text{ F m}^2$  and  $3.4 \times 10^{-40} \text{ F m}^2$  respectively, and the mean ionic polarizability per ion pair is  $6 \times 10^{-40} \text{ F m}^2$ . What is the dielectric constant? (Given that  $N = 1/a^3$ ).

3) In a certain atom, the positive charge in the nucleus has a value of  $q = 3.2 \times 10^{-19} \text{ C}$ , the radius of the atom  $R = 6 \times 10^{-9} \text{ cm}$ ,  $E = 20 \text{ KV/cm}$  and  $N = 3 \times 10^{19} \text{ cm}^{-3}$ . Find the equilibrium distance  $d_E$ , the dielectric susceptibility and dielectric constant resulting from electronic polarization.



4) An atom with a radius of  $5 \times 10^{-8}$  cm has a positive charge in the nucleus with a magnitude of  $4 \times 10^{-18}$  C. If the atom is subjected to an electrical field of 15KV/cm, calculate the equilibrium distance "d" according to the electronic polarization assuming a number of molecules per unit volume of  $25 \times 10^{20}$ . Calculate also the electric dipole moment, the polarization, the dielectric susceptibility and the dielectric constant after equilibrium.

5) Find the polarizability of a certain ion in  $\text{Fm}^2$  assuming that the number of molecules per unit volume is  $22 \times 10^{18} \text{ cm}^{-3}$ . The dielectric constant of the ion is 4.

$$2 = 22 \times 10^{18}$$

$$\epsilon_r = 4$$

$$\frac{\epsilon_r - 1}{\epsilon_r + 2} = \frac{3 \epsilon_0}{3 \epsilon_0}$$

$$\alpha = 6.634 \times 10^{-37} \text{ Fm}^2$$



$$\epsilon_r = 1 + \frac{N \alpha_0}{\epsilon_0} \frac{1}{1 + j\omega\tau} = \epsilon' + j\epsilon''$$

1) For the orientation polarization with sinusoidal applied field, find the expressions for  $\epsilon'_r$  and  $\epsilon''_r$ .

2) With the help of equations 1-6, 1-8 and 2-4, derive equations to describe the variation of the dielectric constant with frequency. Assume that  $\alpha_0 = 6 \times 10^{-36}$  F m<sup>2</sup> and  $N = 25 \times 10^{22}$  m<sup>-3</sup>. Plot this variation when the frequency varies in the range from  $0.001/\tau$  to  $1000/\tau$ .

3) Obtain the dielectric loss per unit capacitance in a capacitor in terms of the loss tangent. Obtain the phase difference between the current through the capacitor and that through  $R_p$ . What is the significance of  $\delta$ ?

4) Calculate the power dissipated per unit volume of cross-linked polyethylene, XLPE (typical power cable insulator) at 60 Hz at a field of  $100 \text{ kV cm}^{-1}$  if  $\epsilon'_r$  and  $\tan \delta$  of XLPE are 2.3 and  $3 \times 10^{-4}$  respectively.

$$P = \omega \cdot \epsilon'' \cdot E^2$$

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